Magdeburg, 02.11.2003

## Exercises to the classes Numerical Methods in Sciences and Technics

## Exercises no. 4 to 10.11.2003

## The solution of exercise 2 is to submit in the exercise classes on Monday, 10.11.2003 !

Statements given in the lecture can be used in the solution of the exercises without proof. All other statements have to be proved.

- 1. Let the coarse grid matrix  $A^{2h}$  be defined by the Galerkin condition. Compute  $A^{2h}$  using the matrix representations of  $I_h^{2h}$ ,  $A^h$  and  $I_{2h}^h$ .
- 2. Consider the fixed point equation (1.5.4) of the coarse grid correction scheme. Show that if u is the solution of Au = f, then u is the fixed point of (1.5.4).
- 3. Let B be a symmetric matrix. Show that  $B(I-B)^n$ ,  $n \in \mathbb{N}$ , is also a symmetric matrix.