Fachbereich Mathematik und Informatik/ Institut für Mathematik
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## Numerik I

## English translation of Übungsserie 10

Attention: Only solutions which provide a comprehensible reasoning will be graded. Every statement has to be argued. You can use results from the lecture. Statments without reasoning won't get any points.

1. Vector field. Sketch the vector field for the ordinary differential equation $y^{\prime}(x)=x^{2}+y^{2}(x)$.

2 points
2. Types of integrable first order ordinary differential equations. Solve the following ordinary differential equations.
a)

$$
y^{\prime}(x)+y^{2}(x)=1
$$

b)
$y^{\prime}(x)+y(x) \cos x=0$,
c) $y^{\prime}(x)=x y^{7}(x)$,
d)

$$
2 y(x) y^{\prime}(x)=x^{2}
$$

## 4 points

3. Solution by substitution. Determine the general solution of

$$
y^{\prime}(x)=(x-y(x))^{2}+1 .
$$

Hint: Find a suitable substitution.
4. Initial value problem with multiple solutions. Demonstrate that solutions of the initial value problem

$$
y^{\prime}(x)=\sqrt{|y(x)|}, \quad y(0)=0
$$

are not unique.
4 points

The exercises should be solved in groups of three or four students. They have to be submitted until Sie Monday, 04.07.2022, 12:00, either in the box of the tutor or electronically.

