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A threestepped coordinated level set segmentation method for identifying atherosclerotic plaques on MR-images

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Abstract

In this work we propose an adapted level set segmentation technique for the recognition of atherosclerotic plaque tissue on magnetic resonance images. The images are 2dimensional cross-sectional images and show different profiles from ex-vivo human vessels with high variability in vessel shape. We used a curvature based anisotropic diffusion technique to denoise the magnetic resonance images. The segmentation technique is subdivided into three level set steps. Hence, the result of every phase serves as constructive knowledge for the next level set step. By analyzing and combining carefully all available channel information during the first and second step we are capable to delineate exactly the vessel walls by using and adapting two well-known level set segmentation techniques. The third step controls an enclosing level set which separates the plaque patterns from healthy media tissue. In this step we introduce a local weighting concept to consider intensity information for conspicuous plaque patterns. Furthermore, we propose the introduction of a maximal shrinking distance for the third level set in the vessel wall and compare the results of the local weighting algorithm with and without the concept of the maximal shrinking distance. The incorporation of locally weighted intensity information into the level set method allows the algorithm to automatically distinguish plaque from healthy media tissue. The knowledge of the maximal shrinking distance can improve the segmentation results and enables to delineate tissue areas where plaque is most likely.

1. Introduction and Motivation

Atherosclerosis is a serious disease affecting the arterial blood vessels. It is a continuous process in which certain substances (e.g. Cholesterol) accumulate within the vessel wall. This accumulation may cause a slow reduction of the vessel lumen causing a deterioration of blood flow during exertion, or – in the case of a "vulnerable" plaque- rupture suddenly causing a closure of the vessel, which leads to a myocardial infarction (heart attack) or stroke. Thus, it is of most importance to discriminate between stable and unstable plaque and predict potential plaque rupture.

With magnetic resonance (MR) imaging (MRI) it is possible to visualize all parts of the body – including the heart and the vessels - with high spatial resolution (typical values for in-plane resolutions in clinical research are about 400 µm x 400 µm for human plaques in coronary arteries and about 500 µm x 500 µm for aorta plaques). It is possible to visualize plaque in larger vessels, such as the aorta and the carotid arteries with state of the art MR scanners and to characterize plaque components. Methods for automatical plaque segmentation of carotid plaque have been proposed [17] and allow for serial assessment of plaque size and its lipid core. Similarly vessel wall imaging of the coronary arteries is possible and first clinical data is available [15, 27, 28]. However, the rapid motion of the coronary arteries in combination with the small vessel size has made plaque characterization in the coronary arteries impossible. Potential future developments will improve spatial resolution, overcome motion artifacts by motion compensation algorithms [13, 16] or specifically enhance those components of a plaque which cause plaque rupture using specific contrast agents [1, 9].

Due to prospective improvements of MR-image resolution we aim to test modern segmentation techniques for higher in-plane resolutions of 79 µm x 79 µm, which is of course five to six times higher than usual. Informations about segmentation success for this type of MR-images should help to estimate the benefit of level set segmentation techniques for plaque images in general. If we expect higher resolutions for aorta or coronary arteries in future, this contribution represents a pioneer work for automatical segmentation of prospective image reolutions. Upcoming, we aim to test iteratively the segmentation techniques for a successive deterioration of in-plane resolutions to determine frontiers for image qualities in automatical image understanding of plaque. Those contributions should improve the adjustment between the research domains of automatic image understanding and biomedical MR-imaging.

Primarily, we applied pixel-oriented classification algorithms (i.e. k-means) and low-level segmentation approaches (i.e. watershed-segmentation, region growing, presegmentation with scale space concepts [10]) for plaque identification, but stated that suchlike approaches failed in most circumstances. To facilitate automatic image analysis and to reduce observer variability we propose a new algorithm for the assessment of plaque images. In contrast to previous methods with probabilistic approaches we provide a technique that subdivides healthy media tissue from plaque with a closed contour into two resulting subparts. This bordering closed contour guarantees an important local closeness to distinguish between plaque and healthy media tissue during the segmentation process.

Atherosclerotic plaques cannot be differentiated on MR-images by the information of gray values alone, but have an associated regional context. We know however, that atherosclerotic plaques are located within or adjacent to the arterial walls. Consequently, we are interested in a segmentation technique that – in a first step- can segment the arterial vessels and then – in a second step- can recognize relevant plaque structures in the vessel walls. Since vessels must present closed loops, we used a segmentation technique based on active contours as an appropriate starting point.

The model of active contours has been introduced by Kass et. al. [14] and represents an explicit form for describing the motion of a closed contour. The algorithm is based on the principle, that a contour continues to move towards the boundaries of an object. This process can be represented by a minimization of an explicit energy function which includes two terms: one for controlling the smoothness of the contour and one to influence the attraction of the contour to the object boundaries. This parametric model has been frequently used and extended for segmentation problems in (bio)medical image segmentation [5, 6, 8, 23, 26, 30].

The classical model of snakes and active contours yields a significant disadvantage of managing certain topological changes during the contour evolution process. Operations like splitting and merging are not possible to represent with this classical approach. Unfortunately, those flexible curve propagations could be of great importance during the segmentation process of detailed medical

shapes especially for the delineation of the outer media border and the recognition of plaque (which we show in detail in chapter 4.2). Caselles et al. [4] associated the classical active contour model with a geodesic flow model which is represented by a partial differential equation based on a mean curvature flow. The energy minimizing problem can be solved by finding the geodesic contour in Riemann space derived from the image. Solving this model with a level set approach provides the contour with the ability of managing the desired topological changes. The contour is now represented implicitly through the level set equation and yields additionally the advantage of having fewer parameters to guide the propagation of the contour. Parameters used in the level set propagation are geometric measures which are independent of the parametrization of the curve. So they are also called geometric active contours where the classical snakes refer to parametric active contours [30].

In the following Chapters we explain a new approach for plaque segmentation including relevant information during the level set propagation. In Chapter 2 we describe the image data we work with and explain how they have been created. In Chapter 3 we inform the reader about the denoising method we used to denoise the MR-images as preprocessing step for our algorithm. In Chapter 4.1 we give a short summary for the theoretical parts of the level set method which are of interst for the subsequential concepts. Chapter 4.2 describes the threestepped level set method in detail shows results of the segmentation of the inner and outer media borders. Furthermore, this Chapter introduces the proposed concepts for the local weighting of conspicuous vessel wall areas and the healthy media border. Chapter 5 illustrates and compares the results for the proposed concepts. Finally, in Chapter 6 we give a summary and a conclusion of this work and summarize our ideas for future work.

2. MR Data Acquisition

Human arterial specimen from the groin (iliac region) were obtained during vessel replacement surgery. After freezing at -80°C, each specimen was warmed up to 30°C in a phosphate buffered solution. Then it was placed in a 15 ml tube which was then filled with 1% agarose solution. The specimen were measured in a 7 Tesla MR-Tomograph (Bruker Germany, PharmaScan). A whole body mouse coil (diameter of 38 mm) was utilized to obtain a 79 µm x 79 µm in-plane resolution and a 110 µm slice thickness. Scan time for four contrasts (PD, T1, T1fatsat, T2) was about 16 hours. The method is described in more detail in [12]. Figure 1 shows an imaging example of 4 channels each with a 256 x 256 matrix size. With those different channels we have the possibility to emphasize special tissue patterns in a certain range.

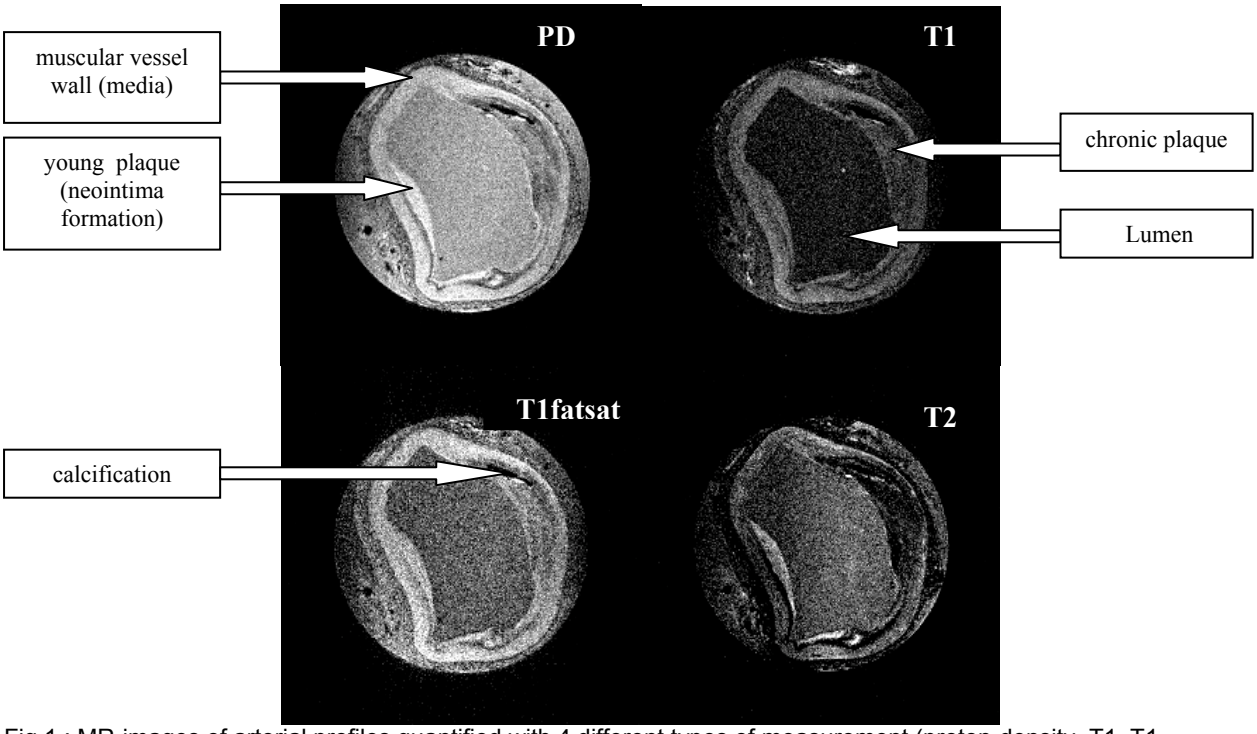

Fig.1 : MR-images of arterial profiles quantified with 4 different types of measurement (proton-density, T1, T1-fatsaturated, T2). The important parts of the arterial profiles are inscribed to the images above.

3. Denoising of MR-images

Although certain relevant plaque patterns are well visible the images exhibit regions with a low signal-to-noise ratio (SNR). The level set propagation is influenced by high image gradients. To ensure a suitable level set propagation we have to denoise those images effectively without loosing too much detail information. Blurring the images with a Gaussian kernel causes an additional dislocation and blurring effect for important edges. Those edges are indispensable information for the stopping decisions of the level set propagation. Consequently, we decided to apply edge-preserving algorithms based on anisotropic diffusion.

A frequently referenced non-linear diffusion model was introduced by Perona and Malik [22]. An extension of the Perona-Malik model (with u representing the underlying image) has been developed by Whitaker and Xue [30], which they call a modified curvature diffusion equation (MCDE):

$$\frac{\partial u}{\partial t} = |\nabla u| \cdot div(g(|\nabla u|) \cdot \frac{\nabla u}{|\nabla u|}) \quad (1)$$

and propose it as a level-set analogon of the anisotropic diffusion model of Perona and Malik. In [29] the authors also empasize its superiority compared to the classical Perona-Malik model. The underlying curve evolution of [29] are the self-snakes, which have been introduced by Sapiro [24].

Due to the fact that we use denoising techniques as a preprocessing step for our work, we choosed the implementation of the ITK development framework [11] to denoise MR images using the MCDE model. The diffusion process can be controlled by the number of iterations and a conductance value, which influences the conductance term of the diffusion process. In the ITK the conductance term [11] is used as a function that can suppress diffusion at higher image gradients and preserve edges by

$$g\left(|\nabla u|\right) = \exp\left(-\frac{|\nabla u|^2}{2k^2}\right) \quad (2)$$

and can be steered by the conductance value k. We used 175 iterations for time steps of 0.125 seconds and denoised the images with conductance values in the range of 1.0 to 2.5.

4. Plaque Segmentation with the Level Set Method

4.1. Description of the Level Set Method

The level set method traces back to the work of Dervieux and Thomasset [7] and has been introduced for the purpose of curve evolution by Osher and Sethian in 1988 [19]. Level set methods gained increasing interest in the field of fluid dynamics and material sciences and became also popular in computer vision fields mainly in medical image processing. (A couple of level set applications are described in [20, 21, 25]). The main idea in the level set concept is describing the subsequent motion of an implicitly given closed contour via a time-dependent partial differential equation (PDE). Instead of dislocating the contour explicitly, what has to be arranged for parametric active contours, we embed the initial location of the two-dimensional front as a zero level set of a three-dimensional function $\phi(x, y, t)$. This function is a signed distance function, which provides for every location in the image its Euclidean distance to the zero level set. Using this definition the resulting movement of the curve is directly related to the temporal dislocation of the zero level (Fig.2).

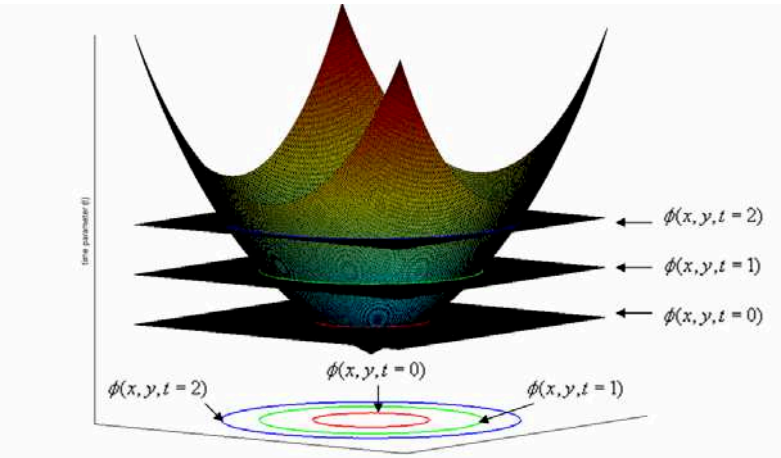

Fig.2 : Embedding a closed contour as a zero level set into a 3D time-dependent function. The 3 resulting zero level sets are shown in 2D with their corresponding colours.

If we calculate the time-dependent alteration of the signed distance function for certain time steps, we can follow the time-dependent displacement of the curve as the zero level set of the signed distance function. The PDE can be solved by using explicit or implicit methods for time discretization. By using explicit methods we have to ensure numerical stability, which can be realized by applying relatively small time steps for the time discretization that fulfill the condition of Courant-Friedrichs-Lewy (CFL condition).

Segmentation techniques using level set propagation and considering image properties (i.e. edge information) and curve properties (i.e. curvature) were suggested by Malladi et. al. [18] and Caselles et. al. [4]. Stopping terms for implicit active contours with mean curvature motion have been introduced in [3]. The authors in [3, 4, 18] propose stopping terms, which are based on image gradients and are represented by the factors:

$$g(u_0) = \frac{1}{1 + \left|\nabla G_\sigma(x,y) * u_o(x,y)\right|^p}, p \geq 1 \quad (3), \qquad g(u_0) = \frac{1}{\exp(\left|\nabla G_\sigma * u_0(x,y)\right|)} \quad (4)$$

with u_0 as the original image and G_σ as the Gaussian function with standard deviation σ. The curvature can be expressed by the divergence of the normal, which can be simplified to the Laplacian, if we ensure the condition $\left|\nabla \phi\right| = 1$. This can be guaranteed by a reinitialization process which aims to renew the signed distances after every time step.

We apply a segmentation technique for the outer media border, which relies upon the principle of Malladi et. al. [18], who introduced curvature and image gradients into the level set propagation via

$$\phi_t + g(u_0) \cdot \left(F_A + F_G\right) \cdot \left|\nabla \phi\right| = 0 \quad (5)$$

where the force F_A represents the force in normal direction for the level set propagation. Depending on the sign of the distance values inside and outside the curve, the sign of F_A can be used to shrink or expand the evolving curve. The other term F_G stands for the geometry of the front such like the local curvature. With the model (5) we can influence a zero level set to stop at the desired boundaries of the object and penalize its local curvature. The penalization of the curvature is important for medical objects, which in general exhibit smoothed boundaries. However, this model requires edge information for the whole boundary of the object which is to be segmented. For medical images the problem of missing edges is well-known, so the application of (5) can lead to the leakage of the zero level set through the gaps caused by missing edges. A possibility to resolve this problem is the geodesic active contour model proposed by Caselles et al. [4]. They show that finding the geodesic curve in Riemannian space is equivalent to solving the classical energy model of the active contours. The geodesic active contour model (6) yields an additional attraction term with respect to (5):

$$\phi_t = g(u_0) \cdot (F_A + F_G) \cdot \left|\nabla \phi\right| + \nabla g(u_0) \cdot \nabla \phi \quad (6)$$

The scalar product of the attraction term $\nabla g \cdot \nabla \phi$ attracts the evolving curve to the boundary, if the curve is near to the boundary. The term can even prevent the leakage of the evolving curve through weak edges and small gaps.

4.2 The Threestepped Level Set Segmentation

The goal of our method is the segmentation of plaque from MR images measured in [12]. The media can exhibit a variety of plaque structures, however those formations arise adjacent or inside the vessel wall. We aim to segment the media together with its plaque tissue and after that delineating healthy tissue from plaque tissue inside the vessel wall.

For the segmentation we used the level set method. The process of our threestepped plaque segmentation can be subdivided in three phases. Every phase uses a single level set approach and the results of every phase serve as additional knowledge for the next level set step. Primarily, we apply an inner zero level set to separate the lumen from the inner media border. After that we evolve the final contour of the first level set phase until it reaches the outer boundary of the media.

The first two steps ensure the segmentation of the media. The most challenging task is the differentiation of plaque from healthy media tissue inside the extracted media. Fortunately, we know that atherosclerosis is a continuous process beginning adjacent to the inner media border. Neointimal formations accumulate at the inner media border and chronic plaque develops successively inside the media. Subsequently, we exploit the closed contour of the zero level set to delineate the healthy media tissue from plaque with a shrinking zero level set starting from the outer media border. This coordinated process will be explained in the following three sections in more detail.

4.2.1. Detecting the Inner Border of the Media

We expect the outer border to be approximatively circle-shaped. In our images of surgical specimen this is not fulfilled due to deformations during surgery and further preparation. The inner border of the vessel can have more variability, but will always form a closed shape with rounded inner edges. In our considerations we exclude vessels with a completely closed lumen. Consequently, the initial seed point was placed in the center of the arterial profile for every image.

On all T1 and T1fatsat images exists more contrast between the media and its adjacent regions in comparison with the corresponding PD and T2 images. To preserve the contrast for the media boundaries we denoised the T1 and T1fatsat images by using a lower conductance value of 1.0. Due to possible artifacts and signal descents during measurement the MR images can loose information and miss edge magnitude. Executing the algorithm for only one channel image could cause leakage effects for the zero level set. We aim to compensate this effect by averaging the intensities from two measurements. Although contrast can be deteriorated in places, we collect sufficient edge magnitude to segment the media by averaging the denoised T1 and T1fatSat images.

For guiding the first level set to the inner media border we used the geodesic active contour model [4] and used (6) in combination with (3) (p=2). Starting from an initial point inside the lumen, the first zero level set terminates its propagation exactly at the inner media borders. Near the inner media border the attraction term attracts the curve to the exact edges of the border and furthermore avoids the leakage into the vessel wall region (s. Fig.3). On its way to the inne rmedia border the zero level set encircles those edges, that result from inhomogenities inside the lumen.

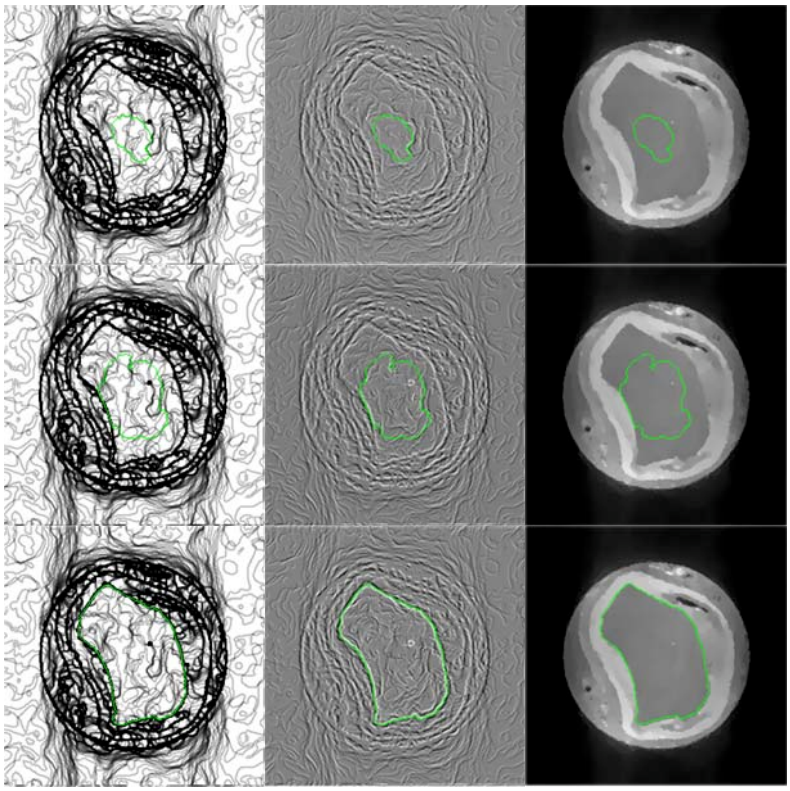

Fig.3: Curve evolution of the geodesic active contour model converging to the inner media border. Three time steps with the zero level set (green curve) are shown . Left: zero level set on edge image relying upon the stopping term (g). Middle: Attraction force ($\nabla g \cdot \nabla \phi$) from the geodesic active contour model. Right: propagating curve on denoised image. (We used propagation speed $F_A = 6$ and curvature speed $F_G = 1$).

4.2.2. Detecting the Outer Border of the Media

It is not possible to segment the outer media border with a shrinking level set starting beyond the media. There could exist parts from other tissues outside of the vessel wall which could unintendedly stop a shrinking zero level set before it reaches the outer media border. After delineating the inner media border there is no reliable knowledge about the extent of plaque and media tissues. Subsequently, it is precarious to estimate an initial position for a shrinking level set beyond the media based upon the location from the delineated inner media border. Hence, we utilize the position of the inner media border as determined in the first step as starting zero level set for the next segmentation step.

Due to higher inhomogenities of plaque tissue inside the vessel wall there exist stronger edges than in the lumen region. For the further propagation we stated that the geodesic active contour model can be attracted by strong edges inside the vessel wall and stop the propagation unintendedly. Hence, we extracted the relevant edges with the Canny algorithm [2] and used Canny edges as stopping criterion. (For the hysteresis in the Canny algorithm we choosed 0.05 as higher threshold and 0.02 as lower threshold for all images). For the second level set step we applied the concept of [18] and used (5) to guide the second level set to the outer media border. For using the flexible motion character of the level sets we set the curvature speed equal to zero ($F_G = 0$), to allow the zero level set to circulate around Canny edges inside the vessel wall. Instead of using (3) or (4) we used Canny edges as stopping term

$$canny(x,y) = \begin{cases} 0 & ,if \quad (x,y) \quad is \quad Canny_edge \\ 1 & ,else \end{cases} \tag{7}$$

To overcome the barricades of the edge of the inner media border we let the zero level set pass by using one iteration without applying the stopping term. Similarly to the first step, we apply the second

segmentation step to the average image of the denoised T1 and T1fatsat images. To exploit the edge enhancement of the anisotropic diffusion we used conductance values of 2.5 to denoise the images. The denoising method preserves all Canny edges of the outer media border and attentuates edges inside the vessel wall.

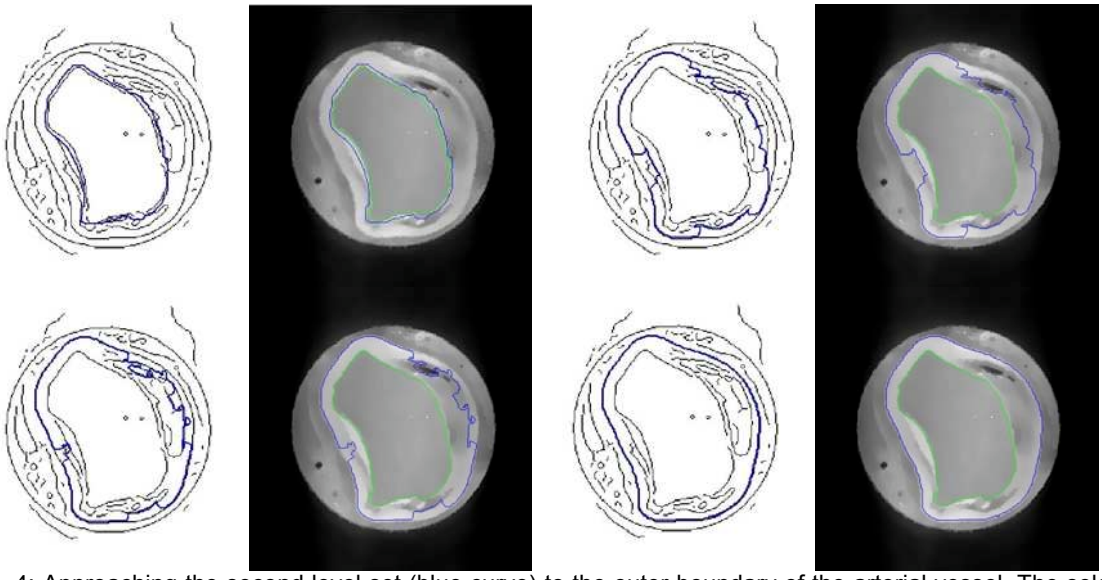

Fig. 4: Approaching the second level set (blue curve) to the outer boundary of the arterial vessel. The selected 4 time steps are listed pairwise. The final zero level set of the inner vessel border is shown in green colour for every time step in the right image. The circumfluent propagation (propagation speeds of $F_A = 2$) along Canny edges can be seen in the left image of every time step.

After this step the whole media is delineated which provides a comfortable initial point for further plaque recognition, because atherosclerotic plaque can only be located adjacent to the inner media border or in the media itself.

4.2.3. Contouring of Atherosclerotic Plaque Patterns in the Media

In contrast to the first and second level set step we need as much information from plaque tissue as possible for the third level set step. Plaque tissue is enhanced in PD and T2 channel images. However, in [9] it was argued that T2 weighted images exhibit most plaque contrast, but also in PD weighted images plaque is enhanced. For collecting as much plaque information as possible we denoised the PD and T2 images with a conductance term of 1.0 and used the average image for the third level set step. To present our results we refer to six different plaque images with (Fig. 5).

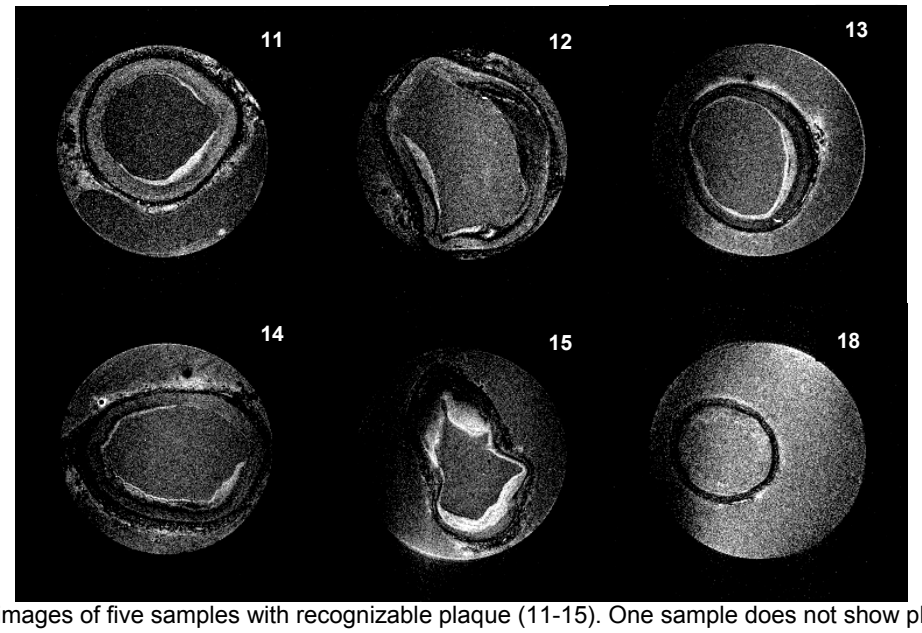

Fig. 5: T2 images of five samples with recognizable plaque (11-15). One sample does not show plaque (18).

The plaque images do not show suitable edge information with respect to the relevant plaque tissue. High gradient magnitudes inside the vessel wall influence the zero level set to stop too early, whereas Canny edges exhibit gaps (Fig. 6). Consequently, we need a further concept, that supports plaque segmentation inside the vessel wall.

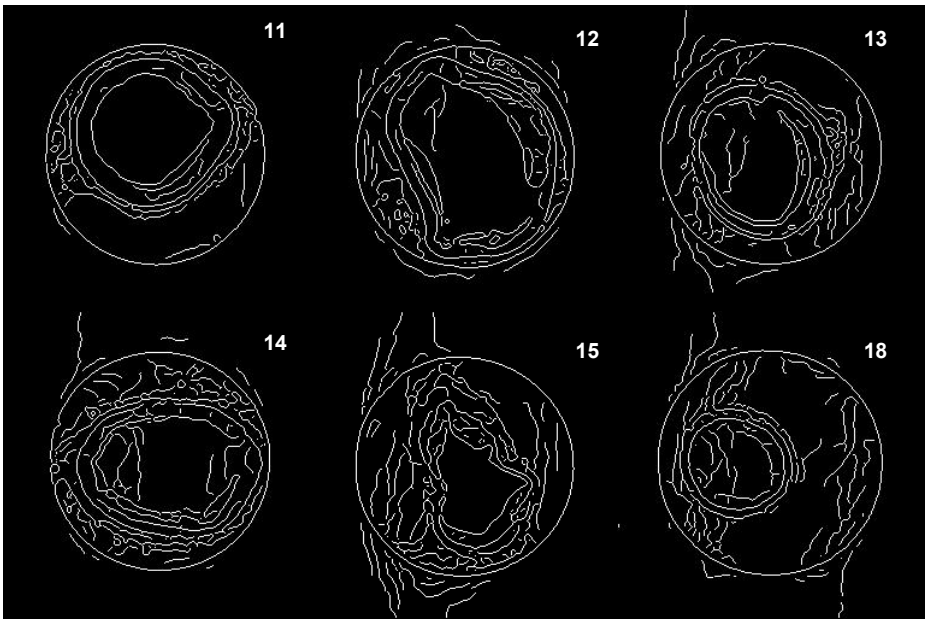

Fig. 6: Canny edges from the average image of the denoised PD and T2 images. The plaque patterns cannot be delineated with Canny edges due to missing edge information and gaps in the progression of canny edges.

4.2.3.1. Penalizing Grayvalue Deviances using a Local Weighting Concept

Regarding the plaque images from Fig. 5 it gets obvious that plaque patterns attract attention also with their distribution of intensity information. Neointimal formations yield higher intensities whereas chronic plaque is darker in comparison with the adjacent healthy media tissue. Thus, we decided to penalize striking intensities additionally to Canny edges during the level set propagation.

To obtain a measure for the intensity distribution of healthy media tissue, we consider the intensities in a small stripe inside the media adjacent to the outer media border. We disregard the case of a media with chronic plaque tangenting the outer media border. We apply a shrinking level set with negative propagation speed (-3) and two iterations to delineate a small stripe between the actual zero level set and the outer media border. However, it is precarious to consider the intensity distribution of the whole stripe to distinguish plaque and healthy media. During MR measurement can arise artifacts and descents of signal intensity in an arbitrary direction. Due to those technical features, it is not predictable, if an intensity at a certain location on the media does represent the same tissue property of another media location. Subsequently, the intensities in the whole stripe are no reliable measure for healthy media intensities. To overcome this challenge we have to incorporate locally weighted intensity information from the stripe into the level set equation.

For every pixel on the outer media border (we call it the reference point) we calculate a weighted average value and an accordant weighted standard deviation. All pixels inside the stripe contribute to the weighted average value and weighted standard deviation of a reference point with their reference distance. The reference distance from a certain point inside the stripe is the length on the outer border between its closest point on the outer border and the reference point. Due to the curvature values for the outer media border, the reference distance ensures an appropriate distance measure for our weighting method. For the construction of the weighted average and the weighted standard deviation for every reference point we provide the weights of the points inside the stripe with a Gaussian weighting function:

$$w(x,y) = \frac{1}{\sigma\sqrt{2\pi}} \cdot \exp(-\frac{d^2(x,y)}{2\sigma^2}) \qquad (8)$$

where d represents the explained reference distance, σ the selectable standard deviation and (x,y) a position of a point on the outer stripe. The weighting procedure can be demonstrated with Fig. 7.

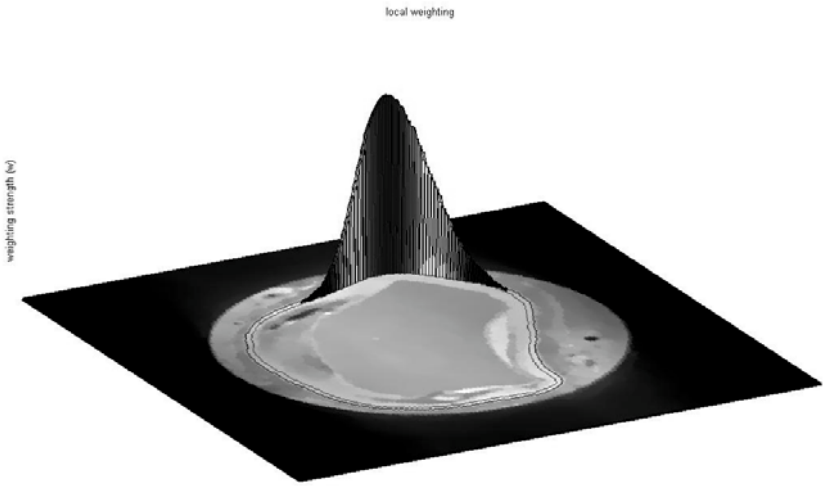

Fig. 7: Local weighting resp. a certain reference point and a selected standard deviation. The weighted values for the pixels inside the stripe based on a selected standard deviation are shown with a thin Gaussian-shaped wall. The reference point and the points on its perpendicular in this stripe have the highest weighted values for the local weighting process.

Choosing a very small standard deviation results in weighting the intensities inside the stripe more locally. By selecting a high standard deviation for the Gaussian weighting function we will integrate more information from the stripe to make a local decision for conspicuous regions. Increasing the standard deviation will converge to a uniformly distributed weighting for all points inside the stripe.

With the local weighting method we determine the dispersion range for healthy media tissue.
The weighted average value $\overline{m(x,y)}$ for every reference point on the outer media border is given by

$$\overline{m(x,y)} = \frac{\sum_{i=1}^{N} w(x_i,y_i) \cdot I(x_i,y_i)}{\sum_{i=1}^{N} w(x_i,y_i)} \qquad (9)$$

where i should be an index referencing all points p_i with location (x_i,y_i) in the outer stripe, $I(x_i,y_i)$ the intensity of (x_i,y_i) and N the total number of points in this stripe. Its corresponding weighted standard deviation is given by:

$$\overline{std(x,y)} = \frac{\sum_{i=1}^{N} w(x_i,y_i) \cdot (I(x_i,y_i) - \overline{m(x,y)})^2}{\sum_{i=1}^{N} w(x_i,y_i) - 1} \qquad (10)$$

Every pixel in the media, which is not located inside the stripe, has a closest point (reference point) on the outer media border. Hence, we compare every pixel intensity in the media, whose pixel is not located inside the stripe, with the dispersion range of its reference point. If the intensity falls inside the range of the weighted standard deviation about the weighted average of the reference point, then this pixel belongs to healthy media tissue. If this is not the case then this intensity is locally striking and belongs to plaque tissue. Consequently, we penalize those intensities exponentially with their distance to the dispersion range of the weighted standard deviation. We express this intensity penalty with:

$$\bar{h}(x,y)=\begin{cases}1 & ,\left|I(x,y)-\overline{m(x_r,y_r)}\right|<\overline{std(x_r,y_r)}\\ \exp(-(\left|I(x,y)-\overline{m(x_r,y_r)}\right|-\overline{std(x_r,y_r)})) & ,else\end{cases} \quad (11)$$

In this context the intensity of an evaluated pixel location $I(x,y)$ is compared with the weighted average $\overline{m(x_r y_r)}$ and weighted standard deviation $\overline{std(x_r,y_r)}$ resp. its reference point (x_r,y_r).

We incorporate the penalty of (11) into the level set equation. Furthermore, we know the pixel locations of the lumen from the first level set step and avoid a possible leakage into the lumen area with the stopping criterion of

$$lumen(x,y)=\begin{cases}0 & ,if \quad (x,y) \quad is \quad lumenposition\\ 1 & ,else\end{cases} \quad (12)$$

Subsequently, our level set equation results in

$$\frac{\partial\phi}{\partial t}=canny\cdot\bar{h}\cdot lumen\cdot F_A\cdot\left|\nabla\phi\right| \quad (13)$$

Due to the fact that edges calculated by Gaussian convolution are very broad, they do not delineate plaque tissue precisely. Canny edges inside the media exhibit gaps, where the zero level set can break through. Furthermore, Canny edges can divide media tissue that is not relevant for plaque recognition. With the local weighting concept we introduce a measure that is independent from edge information and regard local grayvalue distributions which are salint for a human observer. These salient areas are also important for cardiologists to distinguish plaque tissue from healthy media tissue. Hence, the local weighting approach can support Canny edges to delineate plaque tissue. Canny edges which do not delineate conspicuous areas, are encircled by the zero level set.

It should be mentioned that the segmentation results of the local weighting concept can be steered by the selection of the standard deviation σ in (8). Depending on the circumstances of the measurement and the interests of the segmentation, it could be important to incorporate intensities of the stripe which are very close to the reference point. Our purpose was to be independent of the signal descent of the intensities during measurement, so we used values for sigma in the range of 10 to 20. Due to the dependence of the outer stripe for the local weighting it should be clarified that the segmentation results are also dependent on the results of the first and second level set step. If the media was not segmented correctly, the outer stripe could contain intensities of other tissue, which could falsify the local weighting results. With this concept we take into account the shape of the outer border providing the distant values along the level sets.

4.2.3.2. Introduction of the Maximal Shrinking Distance in the Media

Finally, we use an additional information for supporting the segmentation process of plaque. On all MR images there exists at least one position at the inner media border which does not show plaque accumulation. The closest Euclidean distance from such a location to the outer media border serves as an estimation of the healthy media thickness. All tissue located within the outer media border that was not identified as lumen and has a higher Euclidean distance to the outer media border than the healthy media thickness delineates a region where plaque is most likely.

A healthy media without plaque accumulation shows very small alterations of thickness. Hence, we cannot delineate an exact healthy media thickness due to those small thickness alterations. On plaque images, however, we can delineate the most likely plaque region which serves as a good approximation for a healthy media border. We use the healthy media border as a limitation for the shrinking zero level set inside the media. The distance in normal direction from the outer media border to the healthy media border is called the maximal shrinking distance for the zero level set. This distance measure is independent of the vessel wall thickness and can help to avoid the leakage of the

zero level set into plaque regions, which are not penalized by the local weighting concept or delineated by Canny edges.

After delineating the healthy media border, we can decide for every pixel if it is located inside the delineated region. Subsequently, we can determine the maximal shrinking distance for the zero level set with the stopping condition of

$$healthy(x,y)=\begin{cases}0 & ,if \quad (x,y) \quad inside \quad healthy \quad media \quad border \\ 1 & ,else\end{cases} \tag{14}$$

Due to the fact, that the maximal shrinking distance depends on the most narrow position of the vessel wall and orientates itself to the outer media border, it is not necessary to regard the lumen positions given by (12) anymore. We incorporate the knowledge about the maximal shrinking distance into the level set equation and exchange (13) by (14)

$$\frac{\partial \phi}{\partial t} = canny \cdot \bar{h} \cdot healthy \cdot F_A \cdot |\nabla \phi| \tag{15}$$

5. Results

5.1 Results of the local weighting concept

In Fig. 8 we list the results for the examined image numbers (11-15, 18), which we obtained applying the local weighting concept combined with the level set method according to (13) for the third level set step. To compare the quality of the results we regard expert knowledge about the underlying plaque tissue. For measuring purposes the specimen have been fixed with agarose gel, which has been manually removed for further histological examinations. During the histological preparation the vessel form has been extremely altered, so that a registration between histological images and MR-images is a very complicated issue (Fig. 8). Furthermore, histological images and MR-images exhibit different slice thicknesses (110 µm for MR images but 5-10µm for histological images) and due to partial volume effects an automatical registration between those type of images is awkward.

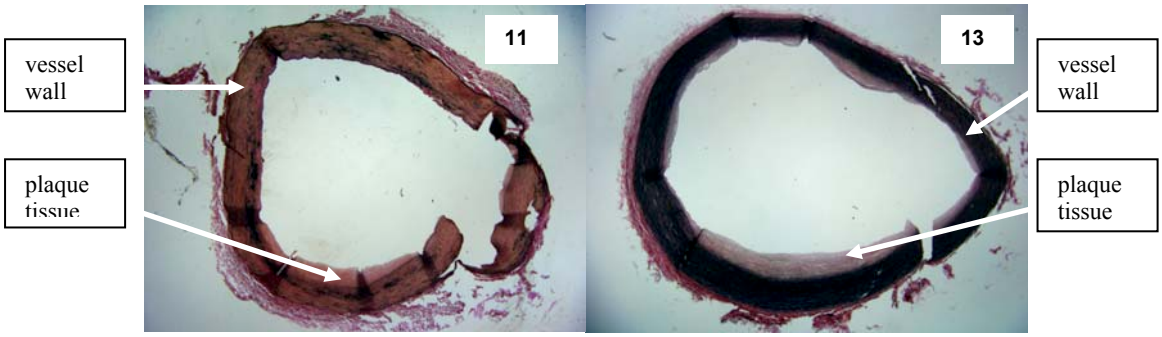

Fig. 8: Histological images for image no. 11 (left) and 13 (right). Plaque tissue (neointima formation) is shown adjacent to the inner media border. The vessel shapes have been modified during histological preparations.

Reliable knowledge for plaque occurence has been introduced by experts after comparing histological images with corresponding MR images. Expert knowledge about plaque regions is shown in Fig. 9 (right column) enclosed by blue curves.

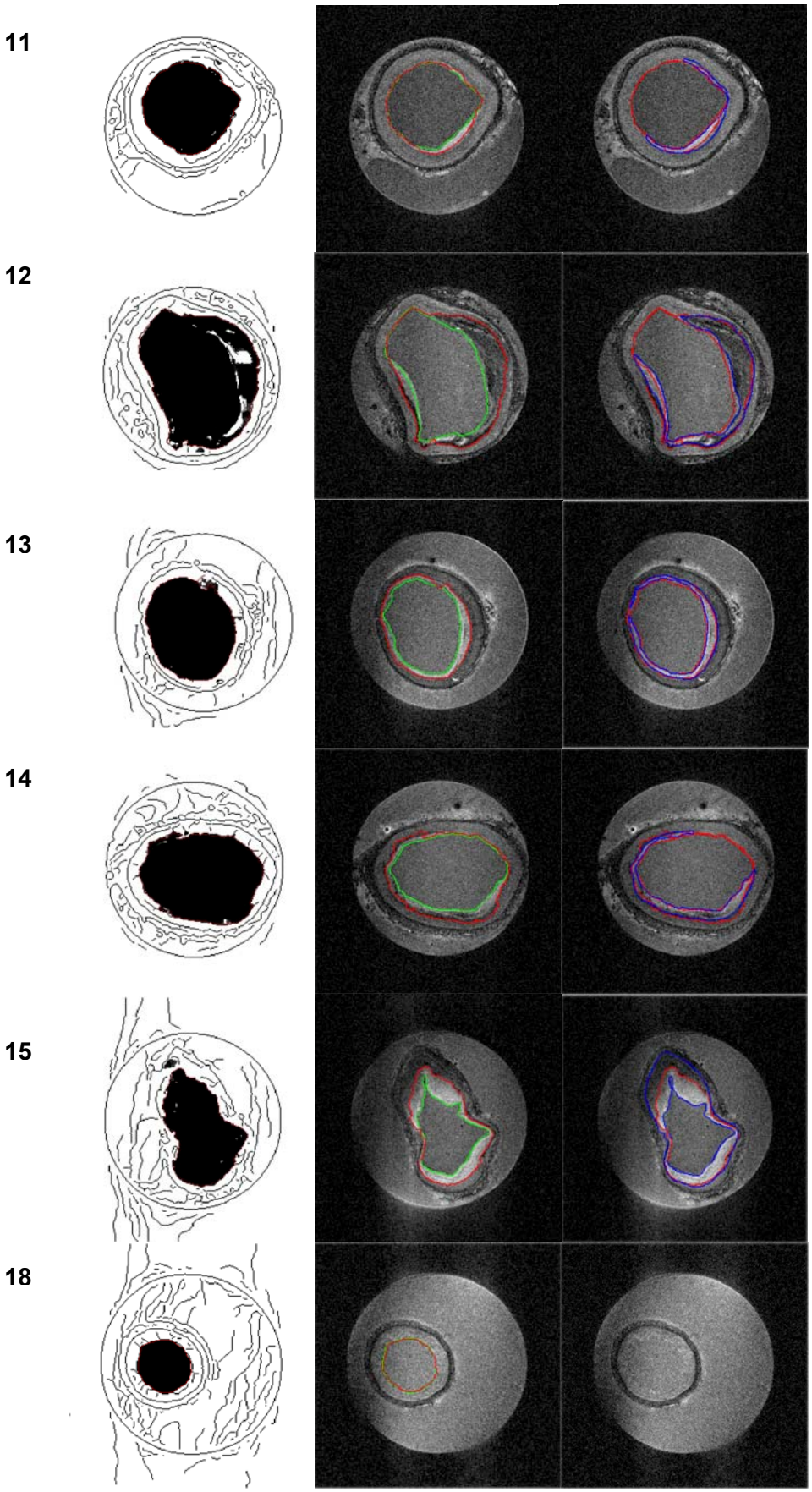

Fig. 9: Final result of the level set propagation with locally weighted deviant areas for all images. Left: local deviant areas with Canny edges and segmented lumen region. Middle: Final zero level set after third level set step (red) and inner media border from first level set step (green). Right: Comparison of result from third level set step (red) with manually evaluated expert knowledge of plaque tissue (blue) (Standard deviation of the weighting function in the range of 10-20).

If Canny edges are connected with delineated plaque the zero level set will stop there. Hence, in some cases, the final closed contour obtains convexities with a thickness of one pixel. Those convexities do not represent plaque. A final mean curvature motion with a curvature penalty of the level sets cannot separate the contour from those convexities due to the closed connection. We know, that Canny edges have a thickness of one pixel [2]. We exploit this knowledge and remove coordinates which occur twice in the final zero level set and get rid of the convexities successfully.

The combination success of Canny edges and local deviant areas to delineate plaque from healthy media tissue gets obvious. Missing edge information is compensated by local deviant plaque areas. On the other hand, plaque intensities which were not evaluated as local deviant, are delineated by Canny edges. Furthermore, Canny edges which do not delineate plaque are encircled by the zero level set. The denoising method removes very thin plaque patterns, hence we loose edge information to stop the level set propagation. However, we regard those thin plaque patterns as not relevant for our segmentation results. Image no. 18 does not exhibit plaque tissue (Fig. 9). There are no conspicuous grayvalue areas inside the vessel wall that could be penalized by our algorithm, hence, for image no. 18 the algorithm does not find plaque.

5.2 Results for the Introduction of the Healthy Media Border in the Local Weighting Concept

The Results for introducing the concept of the healthy media border in our algorithm (according to equation (15)) are shown in Fig. 10.

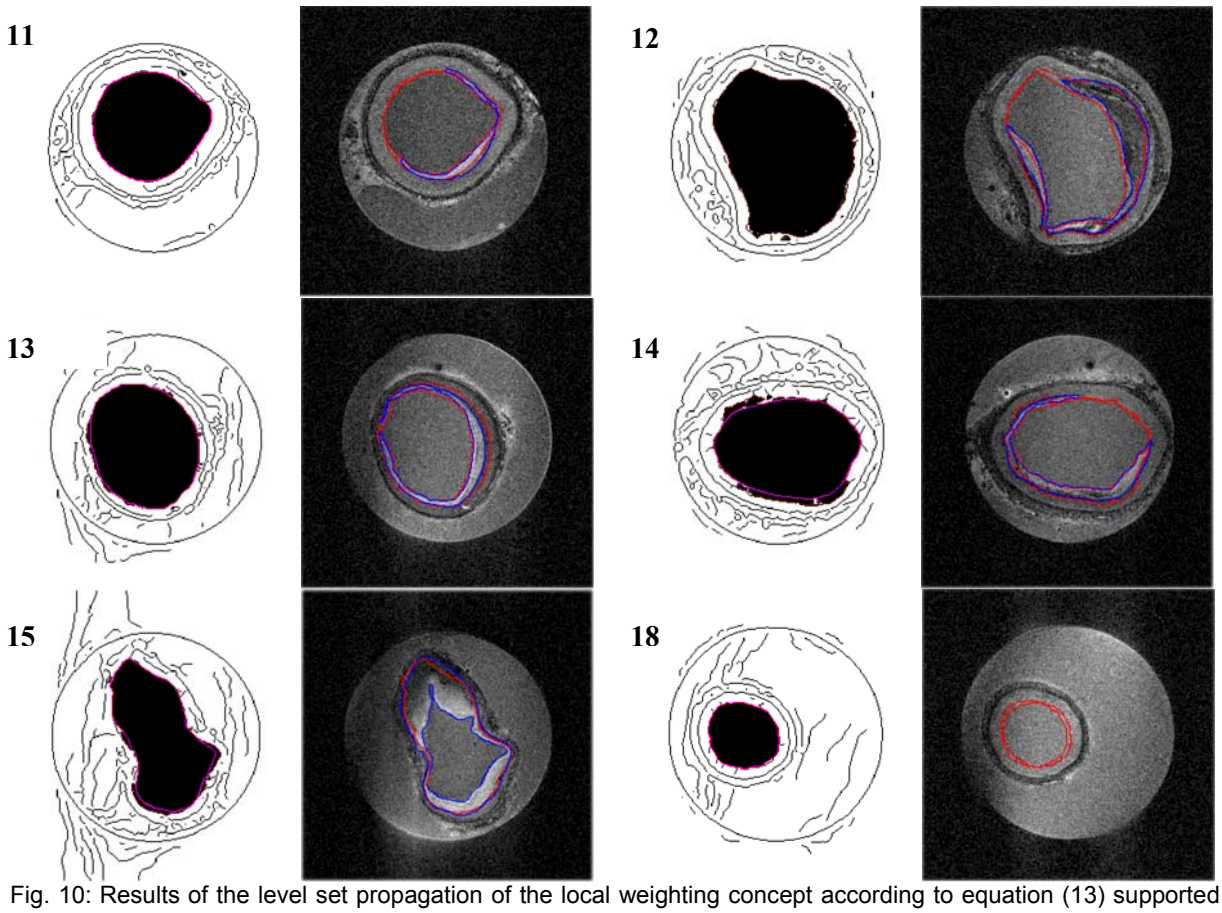

Fig. 10: Results of the level set propagation of the local weighting concept according to equation (13) supported by the healthy media border concept (15).

The maximal shrinking distance avoids the leakage of the zero level set into plaque regions, which are not identified by the deviant intensity areas and furthermore not delineated by Canny edges (Please compare the results for image numbers 11-13 in Fig. 9 and 10). Obviously, the healthy media border

serves as a helpful information to improve the segmentation results especially for vessel wall abnormalities which is not demarcated by different signal levels in the MR images and thus cannot be recognized by a human observer (Please note the result for image no. 15 in Fig. 10).

Such local alterations of vessel wall occur frequently in humans and are not yet regarded as plaques, but described as positive remodeling (Glagov-effect). Those regions represent areas, where plaque accumulation begins as expected and plaque tissue is most likely. For MR images without plaque occurence (i.e. image no. 18) the application of the maximal shrinking distance could show plaque, which indeed represents vessel wall abnormalities. Subsequently, in images without plaque the healthy media border does not detect plaque tissue, but reveals vessel wall abnormalities, where plaque is most likely.

5.3 Comparison of the Results

For analyzing the segmentation result we compared the segmented regions between the inner media border and the final zero level set of the third level set step with the expert knowledge about plaque for every image. We relate the sum of the incorrectly segmented areas to the arterial area which represent the relative segmentation errors as shown in Fig. 11. The local weighting algorithm without taking the healthy media border into account yields error rates lower than 8 %, except for image no. 15, where plaque tissue in the upper part of the media is difficult to distinguish in the MR images. A comparison with the histological image image no. 18 does not show plaque, consequently our algorithm does not find plaque in the MR image.

For evaluating the segmentation results it should be mentioned, that the denoising technique influences the segmentation results by removing thin plaque tissue structures which consequently cannot be delineated by the level set algorithm applied to the denoised images. Furthermore, the segmentation results are influenced by the indistinct media areas which seem to be plaque and have been recognized by our algorithm, but cannot be determined unambiguously as plaque in the histological images (Fig.8).

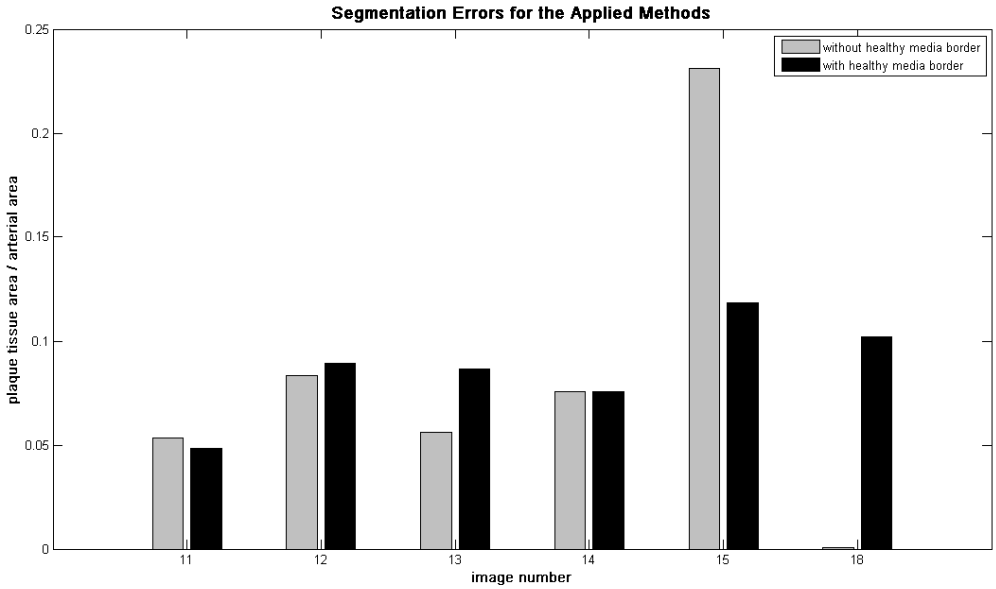

Fig. 11: Segmentation errors with respect to the area of the arterial profiles for the analyzed images. The two applied methods are compared.

Regarding the results of Fig. 11, an unambiguous recommendation using the healthy media knowledge for the examined type of MR-images is not possible yet. It can be seen from Fig. 10 that the healthy media border can prevent the leakage of the zero level set into plaque regions, in the case of missing edges or missing local deviant areas. Otherwise, it can influence the shrinking level set to delineate media tissue, that cannot be identified as plaque in the histological images. For images no. 11 and 15 the healthy media border can reduce the segmentation error, whereas for images no. 12

and 13 this is not the case. In the case of images no. 12 and 13 the healthy media border delineates media areas which could be plaque, but which is difficult to evaluate from histological images. In image no. 15 the healthy media border reduces the segmentation error, because the plaque tissue is not conspicuous in the upper part of the vessel wall and cannot be seen in the MR images (T2 image in Fig. 5). In that case the application of the local weighting concept exclusively is inferior to the combined application together with the healthy media border.

Generally, we recommend the application of the local weighting concept with and without the maximal shrinking distance. Especially for images without plaque (image no. 18) the application of the algorithm without the maximal shrinking distance controls, if the algorithm with maximal shrinking distance just detected vessel wall abnormalities. Furthermore, this strategy delivers the extent of vessel wall abnormalities for images that do not show plaque tissue.

For the application of a maximal shrinking distance, an exact demarcation of the healthy media border is required. It is not determinable, if during preparation the vessel wall thickness has been altered locally. This influences the delineation quality of the healthy media border (e.g. for image no. 13). For evaluating this concept more image data has to be analyzed, however for this work only the examined image data was available. But we think, that the concept to consider a healthy media border for improving the segmentation quality is very important for further research. In future we expect similiar image data but with lower SNR and more preserved vessel shapes, what should make the results more comparable.

6. Conclusion

We explained the preparation and measurement of the MR images we are working with in more detail in Chapter 2. In Chapter 3 we described the denoising technique we used to denoise the MR images and prepare them for the level set propagation. At the beginning of Chapter 4 we give theoretical backgrounds of the level set method. In the main part of this chapter we present our method for the threestepped level set segmentation. For the first level set step we use the geodesic active contour model and determine an initial seed point inside the lumen (which should be determined automatically by applying the Hough transformation for circle detection in future work). The geodesic active contour propagation guides the first extending zero level set towards the exact boundaries of the inner media border. Due to strong intensity gradients from plaque inside the media we adapt a level set technique [18] for Canny edges instead of using the geodesic active contour concept. Basing on the final demarcation from the first level set step we let the zero level set from the second step converge towards the outer media border circulating around the thin Canny edges from plaque tissue. To segment the media, we apply the level set technique on averaged and denoised T1 and T1fatsat images, which exhibit sufficient edge magnitudes for approaching the inner and outer media border with the zero level set.

The third level set step is based on the knowledge of the already segmented inner and outer media border which we collected during the first and second level set segmentation phases. By shrinking the zero level set, which is initially identical with the determined outer media border, we approach towards the Canny edges of the denoised average image derived of plaque relevant PD and T2 channels. Additionally, we propose a method to emphasize areas with higher locally weighted intensity deviances to detect conspicuous plaque patterns. This local weighting approach serves as a filter for plaque intensities and is used as a further stopping criterion for the third zero level set. The local weighting concept evades the problem of intensity attenuation along arbitrary directions in the image, which arises during the MR measurement of the analyzed MR images. Furthermore, we are able to emphasize local distinctive features by adjusting a new parameter for the standard deviation of the local weighting function.

Finally, we justify the introduction of the healthy media border and incorporate this knowledge into the level set equation. This leads to a maximal shrinking distance for the third zero level set and can help to distinguish plaque from healthy media tissue.

The results of the local weighting concept are shown in Chapter 5, where we list the segmentation errors based upon expert knowledge about plaque tissue for every examined image. The results show that segmentation errors are in the range from 4,8% to 11% relating to the arterial profile areas (with one outlier result with 23% segmentation error). We give reasons for the results and show that the healthy media border can improve the segmentation quality, but explain that in future more image data has to be analyzed to compare the results.

The application of the threestepped level set segmentation method show good results, although the available MR images are highly noisy and have been influenced by certain preparations before their measurement in a modern MR tomograph. Due to these circumstances we think, that adapted level set strategies for plaque recognition will also yield useful segmentation results for worse in-plane resolutions from upcoming in-vivo plaque measurements. We aim to encourage for the application of level set methods that use special knowledge during the propagation (like the concept of the healthy media border). We concentrate on level set segmentation with prior shape in future, when more images of similiar types of ex-vivo plaque images (which we analyzed in this work) are available.

In future work, we aim to improve the denoising methods to preserve thin plaque structures, which can be removed unintendedly by using the anisotropic diffusion technique. To preserve all thin plaque structures we applied the level set technique on the original noisy images. Unfortunately, the level set propagation stopped too early due to high image gradients caused by low SNR. Although those thin plaque patterns are actually of minor relevance we aim to enhance the denoising results, which serves as an important preprocessing step for the application of the level set segmentation and influences the segmentation results.

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